## Financial Mathematics

Lagrange multipliers and constrained approximation

0040-1. Maximize $2 x-4 y$ subject to the constraint $x^{4}+16 y^{4}=1$.
0040-2. Minimize $-x+9 y$ subject to
the constraint $x^{6}+y^{6}=1$.
0040-3. a. For every integer $n \geq 1$,
Let $(x, y)=\left(a_{n}, b_{n}\right)$ maximize

$$
y-x \text { subject to }
$$

the constraint $x^{2 n}+y^{2 n}=1$.
Find $\left(a_{n}, b_{n}\right)$.
b. Compute $\lim _{n \rightarrow \infty}\left(a_{n}, b_{n}\right)$.

