Financial Mathematics

The Triangular Central Limit Theorem

0064-1.

Let $W_1^{(1)}$ be a binary PCRV, with uptick/downtick probabilities: $p^{(1)}, q^{(1)}$

Let $W_1^{(2)}, W_2^{(2)}$ be iid binary PCRVs, with uptick/downtick probabilities: $p^{(2)}, q^{(2)}$

Let $W_1^{(3)}, W_2^{(3)}, W_3^{(3)}$ be iid binary PCRVs, with uptick/downtick probabilities: $p^{(3)}, q^{(3)}$ etc., etc., etc. $\forall \text{integers } n \geq 1, \text{ note that } p^{(n)} + q^{(n)} = 1 \text{ and }$

let $X^{(n)} := W_1^{(n)} + \dots + W_n^{(n)}$.

Say $p^{(n)} \to 0.05$.

 $E[X^{(n)}] \to 0.01$, $SD[X^{(n)}] \to 0.45$, as $n \to \infty$. Compute $\lim_{n\to\infty} E[(e^{2X_n}-3)_+]$.