MATH 1271 Fall 2013, Midterm #1 Handout date: Thursday 10 October 2013

PRINT YOUR NAME:

PRINT YOUR TA'S NAME:

WHAT RECITATION SECTION ARE YOU IN?

Closed book, closed notes, no calculators/PDAs; no reference materials of any kind. Turn off all handheld devices, including cell phones.

Show work; a correct answer, by itself, may be insufficient for credit. Arithmetic need not be simplified, unless the problem requests it.

I understand the above, and I understand that cheating has severe consequences, from a failing grade to expulsion.

SIGN YOUR NAME:

I. Multiple choice

A. (5 pts) (no partial credit) Compute $\lim_{x\to-\infty}\left[\frac{x^8+2x^3-4x^2}{2x^4-7x^2}\right]$. Circle one of the following answers:

- (a) 1/2
- (b) -1/2
- (c) ∞
- (d) $-\infty$
- (e) NONE OF THE ABOVE

B. (5 pts) (no partial credit) Compute $[d/dx][(\sin x)e^x]$. Circle one of the following answers:

- (a) $(\cos x)(xe^{x-1})$
- (b) $(\cos x)e^x$
- (c) $(\cos x)e^x + (\sin x)e^x$
- (d) $(\cos x)e^x + (\sin x)(xe^{x-1})$
- (e) NONE OF THE ABOVE

C. (5 pts) (no partial credit) Which is the intuitive definition of $\lim_{x\to 8^+} (H(x)) = \infty$? Circle one of the following answers:

- (a) If H(x) is very positive, then x is close to 8.
- (b) If x is close to 8, then H(x) is very positive.
- (c) If x is close to 8, but greater than 8, then H(x) is very positive.
- (d) If x is close to 8, but not equal to 8, then H(x) is very positive.
- (e) NONE OF THE ABOVE

D. (5 pts) (no partial credit) Compute $[d/dx][3x^4 + 2x^{1/2} + \pi]$. Circle one of the following answers:

- (a) $4x^3 + x^{-1/2}$
- (b) $12x^3 + x^{-1/2}$
- (c) $12x^3 + x^{1/2} + \pi$
- (d) $3x^3 + x^{1/2} + \pi$
- (e) NONE OF THE ABOVE

E. (5 pts) (no partial credit) What is the smallest number x such that $|x-3| \le 0.002$? Circle one of the following answers:

- (a) -2.998
- (b) 3
- (c) 3.002
- (d) 2.998
- (e) NONE OF THE ABOVE

F. (5 pts) (no partial credit) Compute $[d/dx][2e^x + 5\pi]$. Circle one of the following answers:

- (a) $2e^x + 5$
- (b) $2xe^{x-1} + 5$
- (c) $2e^x + 5\pi$
- (d) $2xe^{x-1} + 5\pi$
- (e) NONE OF THE ABOVE

II. True or false (no partial credit):

a. (5 pts)
$$\frac{d}{dx} \left[\frac{\sin x}{x^2} \right] = \frac{\cos x}{2x}$$
.

b. (5 pts) If f is a polynomial of degree 7, then f'' is a polynomial of degree 5.

c. (5 pts)
$$\lim_{x\to 0} \frac{\sin^2 x}{x^2} = 1$$
.

- d. (5 pts) If two functions have the same derivative, then they must be equal.
- e. (5 pts) If f and g are continuous at 3, then f^2g^3 MUST be continuous at 3 as well.

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VERSION D

- I. A,B,C
- I. D,E,F
- II. a,b,c,d,e
- III. 1
- III. 2
- III. 3
- III. 4

III. Computations. Show work. Unless otherwise specified, answers must be exactly correct, but can be left in any form easily calculated on a standard calculator.

1. (10 pts) Compute

$$\frac{d}{dx}\left(\left[\frac{x^2}{1+e^x}\right]\left[5+\sin x\right]\right).$$

2. (15 pts) Compute $\lim_{n\to\infty} \left(1 + \frac{0.05}{n}\right)^n$.

3. (10 pts) Find all horizontal asymptotes to

$$y = \frac{\sqrt{4x^6 + 4x + 4}}{9x^3 + 4}.$$

(NOTE: A horizontal asymptote is a line; your answers should be equations of lines, ${\bf NOT}$ numbers.)

4. (10 pts) Suppose f(0) = 4 and f'(0) = 7. Suppose g(0) = 3 and g'(0) = 5. Let h = fg. Compute h(0) and h'(0).