MATH 1271 Section 30 Recitation Quiz 9

Grader: Cihan Bahran

Time limit: 20 minutes

TA:

Name:

NO CALCULATORS. NO HANDHELD DEVICES. NO BOOKS OR REFERENCE MATERIALS OF ANY KIND.

1. (35 points) Evaluate the limit

$$\lim_{n \to \infty} \left(\frac{1}{n} \sum_{j=1}^n \frac{1}{1 + \frac{j^2}{n^2}} \right)$$

by first converting it to a definite integral.

2. (10 points) Is the following statement true or false?

Both $\frac{\sec^2 x}{2}$ and $\frac{\tan^2 x}{2}$ are anti-derivatives of the function $(\sec^2 x)(\tan x)$.

True False

3. (20 points) Consider the function

$$f(x) = \int_0^x (t^2 - 5t + 6)dt.$$

Which of the following tables describes the maximal intervals of increase and decrease for f?

A)
$$\frac{x \le 2 \quad 2 \le x \le 3 \quad x \ge 3}{\text{inc.} \quad \text{dec.} \quad \text{inc.}}$$

B)
$$\frac{x \le 2.5 \quad x \ge 2.5}{\text{inc.} \quad \text{dec.}}$$

C)
$$\begin{array}{c|c} x \leq 2 & 2 \leq x \leq 3 & x \geq 3 \\ \hline \text{dec.} & \text{inc.} & \text{dec.} \end{array}$$

D)
$$\frac{x \le 2.5 \quad x \ge 2.5}{\text{dec.} \quad \text{inc.}}$$

4.(35 points) Compute the indefinite integral

$$\int \left(e^{6x} + \cos(x/5) + \frac{x^4 + 2x^3 + 8}{\sqrt{x}} \right) dx$$