1. Let $M$ and $N$ be a closed, connected manifolds of dimensions $m$ and $n$. Show that if $m \neq n$, then $M$ and $N$ are not homotopy equivalent.

2. Let $X$ be a closed, connected, non-orientable 3-manifold. Prove that $\pi_1(X)$ is an infinite group.