

Some helpful formulas

$\cos x \cos y = \frac{1}{2}[\cos(x - y) + \cos(x + y)]$	$\tan^2 x + 1 = \sec^2 x$	$1 + \cot^2 x = \csc^2 x$
$\sin x \cos y = \frac{1}{2}[\sin(x - y) + \sin(x + y)]$	$\sin^2 x + \cos^2 x = 1$	$2 \sin^2 x = 1 - \cos(2x)$
$\sin x \sin y = \frac{1}{2}[\cos(x - y) - \cos(x + y)]$	$2 \sin x \cos x = \sin(2x)$	$2 \cos^2 x = 1 + \cos(2x)$
$\int \sec x \, dx = \ln \sec x + \tan x $	$\int \tan x \, dx = \ln \sec x $	$\int \frac{1}{\sqrt{a^2 - x^2}} \, dx = \sin^{-1} \left(\frac{x}{a} \right)$
$\int \csc x \, dx = \ln \csc x - \cot x $	$\int \cot x \, dx = \ln \sin x $	$\int \frac{1}{x^2 + a^2} \, dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right)$
$L = \int_a^b \sqrt{1 + \left[\frac{dy}{dx} \right]^2} \, dx$	$\bar{x} = \frac{1}{m} \sum_{i=1}^n m_i x_i$	$\bar{x} = \frac{1}{A} \int_a^b x f(x) \, dx$
$S = \int_a^b 2\pi y \sqrt{1 + \left[\frac{dy}{dx} \right]^2} \, dx$	$\bar{y} = \frac{1}{m} \sum_{i=1}^n m_i y_i$	$\bar{y} = \frac{1}{A} \int_a^b \frac{1}{2} [f(x)]^2 \, dx$
$P(t) = \frac{M}{1 + Ae^{-kt}}, \quad A = \frac{M - P_0}{P_0}$	$I(x) = e^{\int P(x) \, dx}$	$y_n = y_{n-1} + hF(x_{n-1}, y_{n-1})$
$x = r \cos \theta, y = r \sin \theta$	$A = \int_a^b \frac{1}{2} [f(\theta)]^2 \, d\theta$	$L = \int_a^b \sqrt{r^2 + \left[\frac{dr}{d\theta} \right]^2} \, d\theta$
$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$	$L = \lim_{n \rightarrow \infty} \sqrt[n]{ a_n }$	$c = \lim_{n \rightarrow \infty} \frac{a_n}{b_n}$
$L = \lim_{n \rightarrow \infty} \left \frac{a_{n+1}}{a_n} \right $	$\sum_{n=0}^{\infty} x^n = \frac{1}{1 - x}$	$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$
$\sin x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$	$\cos x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!}$	$\tan^{-1} x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{2n+1}$
$\ln(1+x) = \sum_{n=1}^{\infty} (-1)^{n-1} \frac{x^n}{n}$	$(1+x)^k = \sum_{n=0}^{\infty} \binom{k}{n} x^n$	$\sum_{n=0}^{\infty} \frac{f^{(n)}(a)}{n!} (x-a)^n$
$\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \mathbf{b} \cos \theta$	$\text{proj}_{\mathbf{a}} \mathbf{b} = \frac{\mathbf{a} \cdot \mathbf{b}}{ \mathbf{a} ^2} \mathbf{a}$	$ \mathbf{a} \times \mathbf{b} = \mathbf{a} \mathbf{b} \sin \theta$