1. (8 points) Prove that every infinite set $S$ is equinumerous with a proper subset of itself. (Note: you may not assume the set $S$ is countable.)
2. (7 points) Prove that for every natural number $n$,

$$(2)(6)(10)(14)\cdots(4n-2) = \frac{(2n)!}{n!}.$$