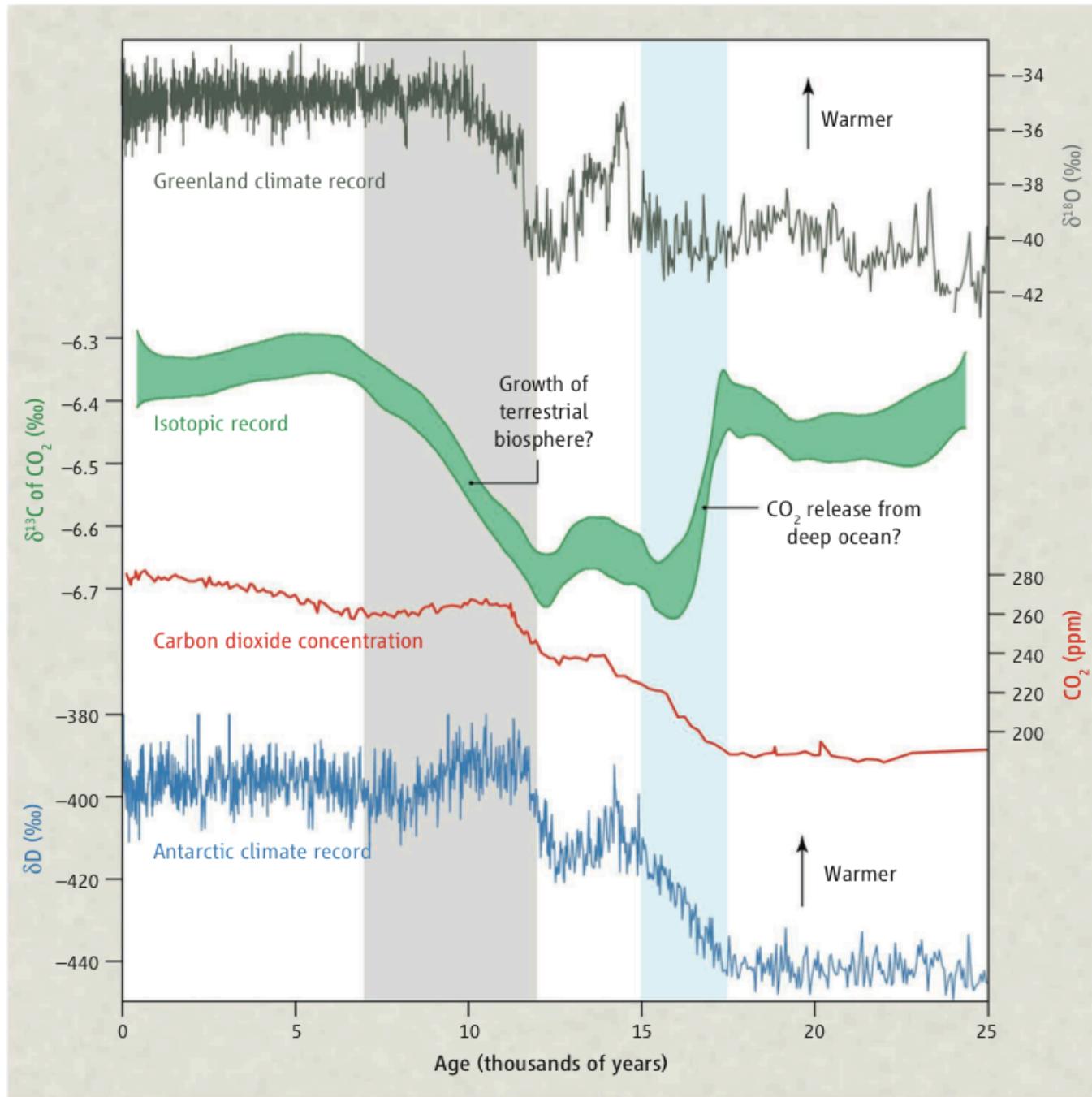


Peatland Constraints on the Deglacial CO₂ Rise from Ice Cores

Alice Nadeau

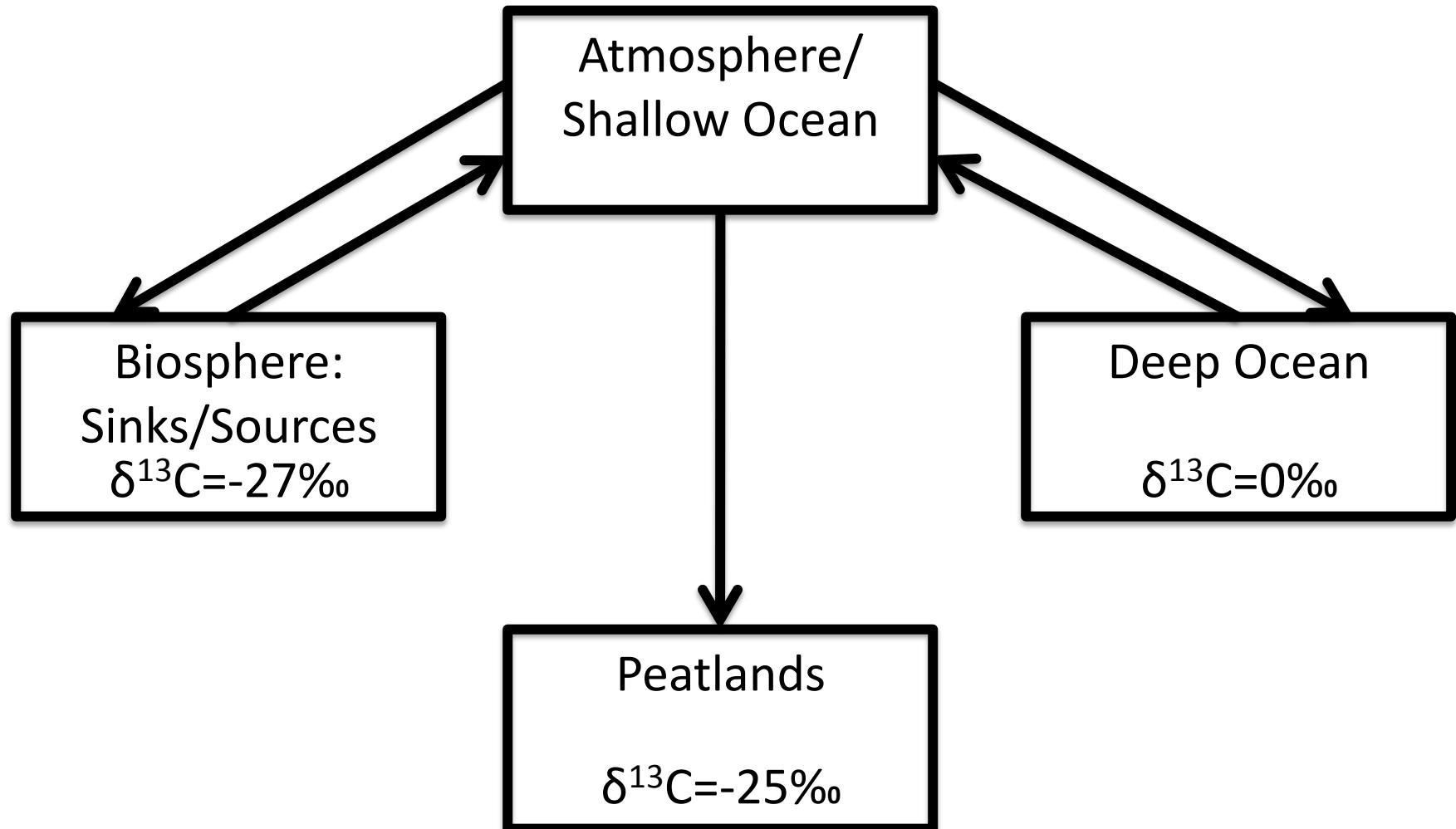
University of Minnesota



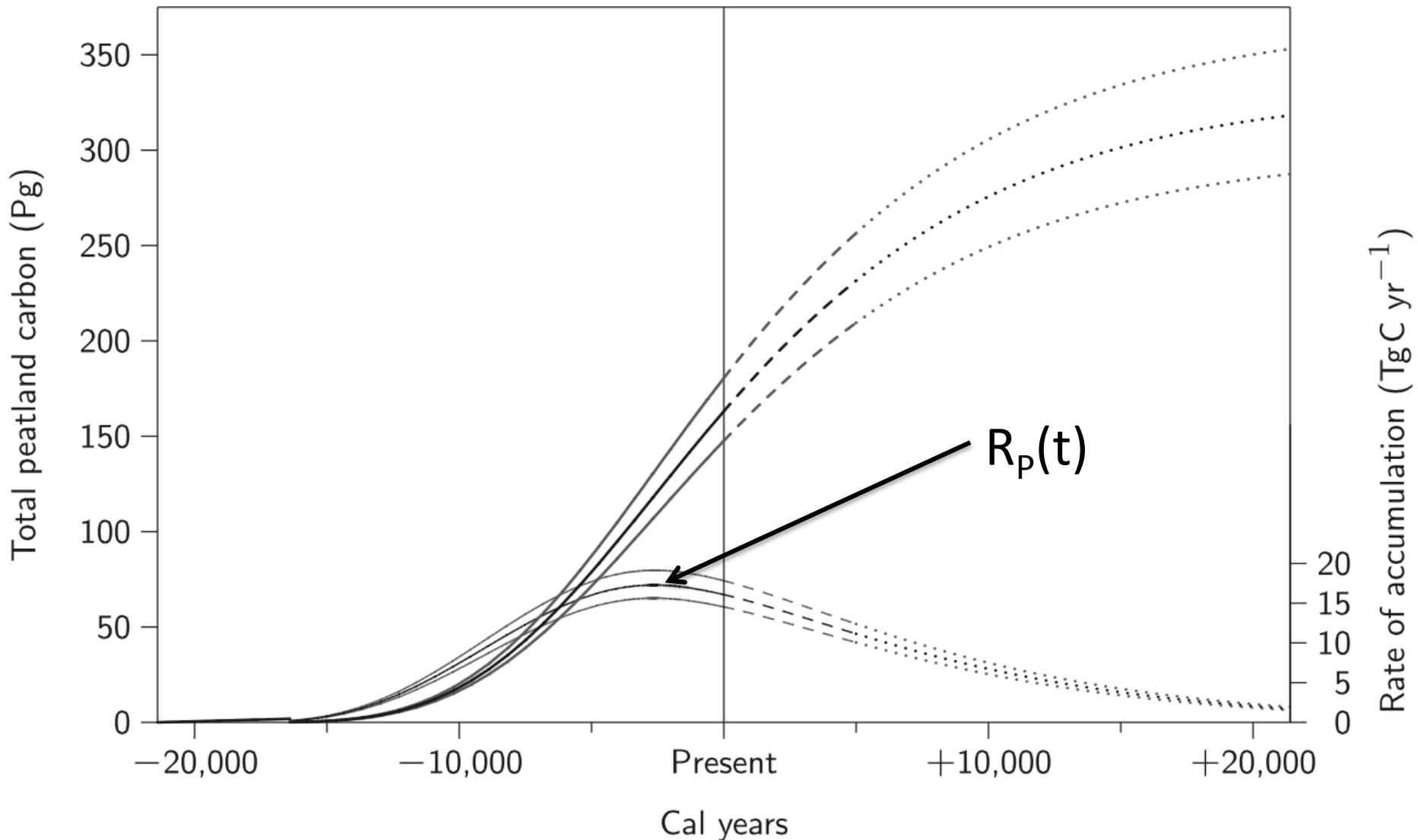
Brook, E. *Science*: 336 pg. 682-683.

Possible Factors

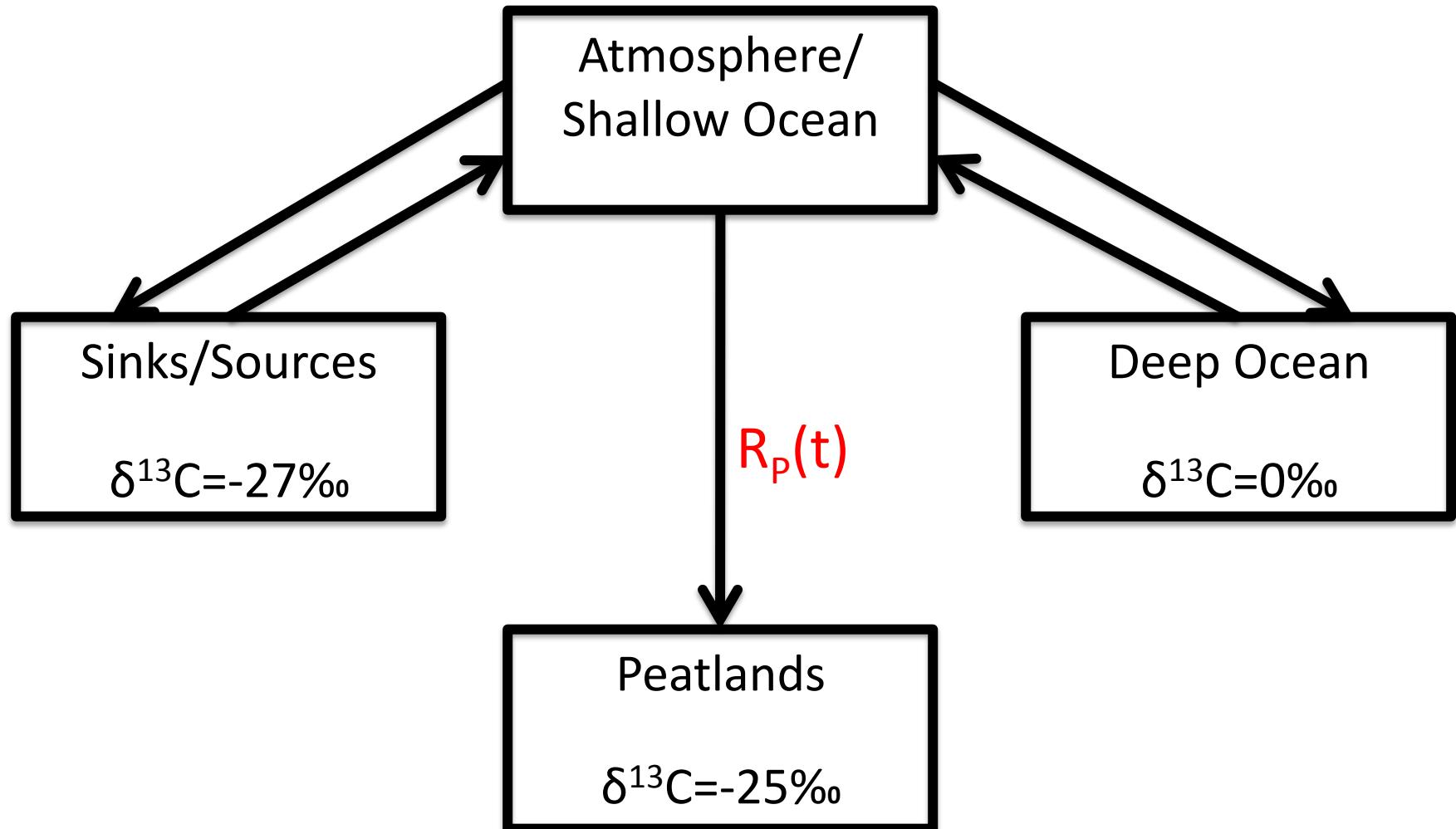
- CO₂ Sources
 - Melting dirty glaciers
 - Coastal ocean rise
 - Loss of grasslands/forests (Sahara/Australia)
- CO₂ Sinks
 - Peatlands
 - Lake Sediments
 - Boreal Forests
 - Coral Reefs



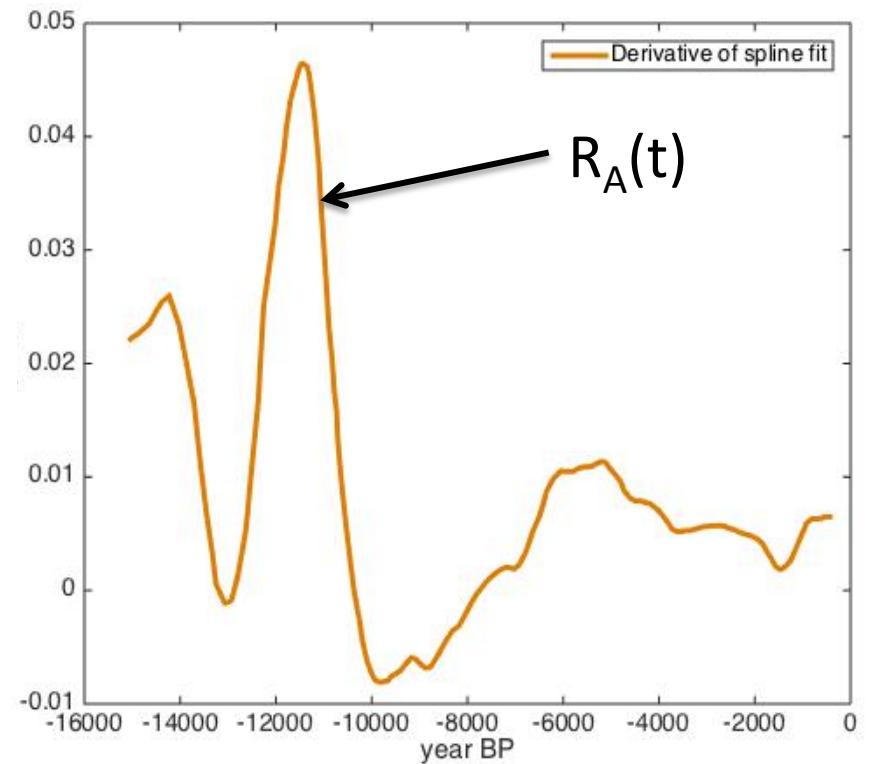
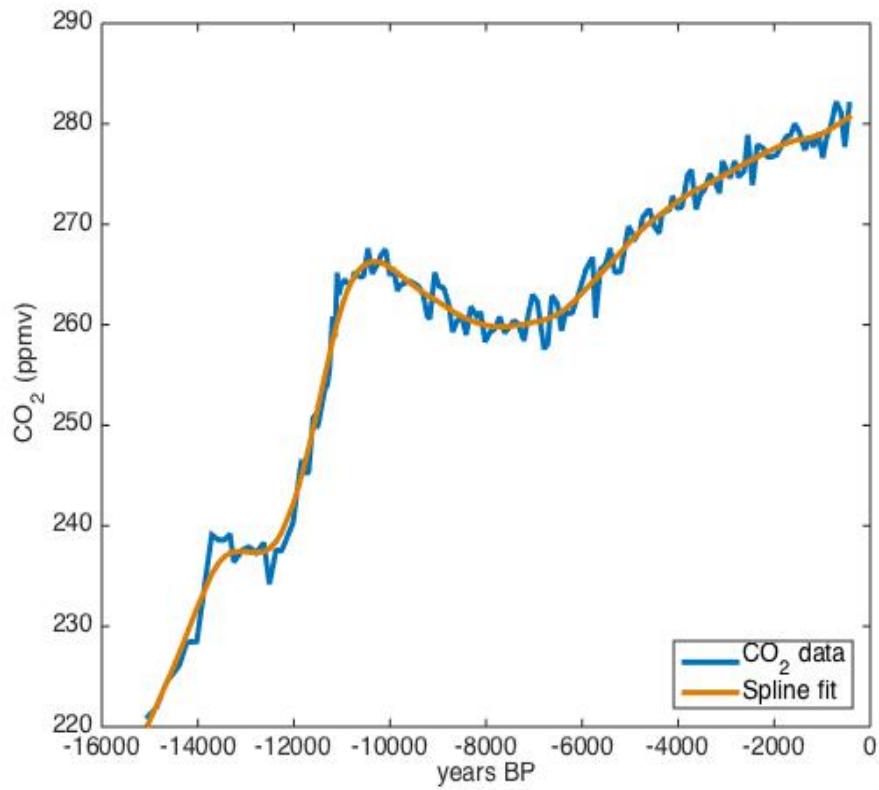
Rate of Peatland Growth

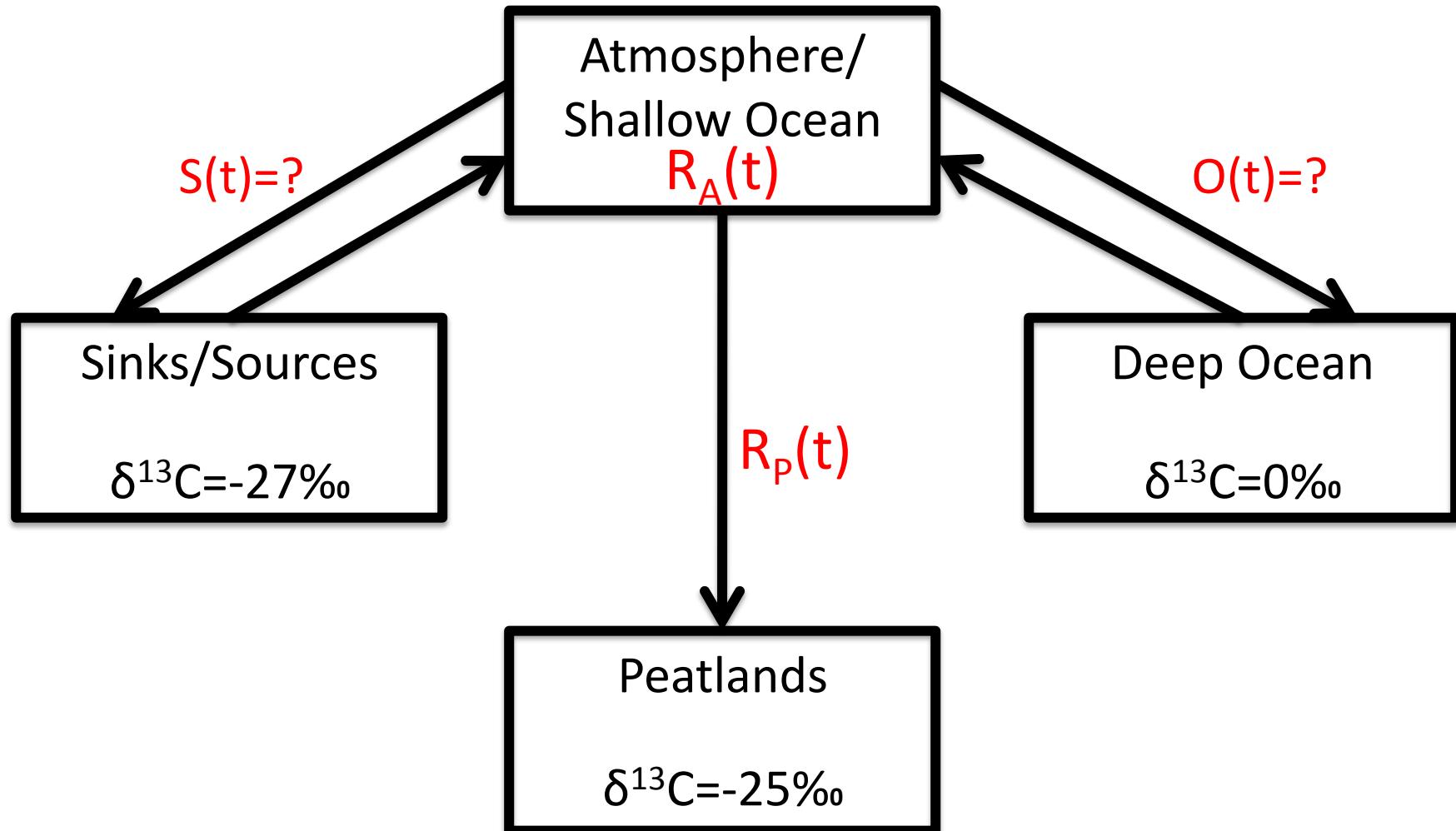


Gorham, E. et al. *Qua. Sci. Rev.*: **58** pg.77-82.



Rate of Atmospheric Carbon Change



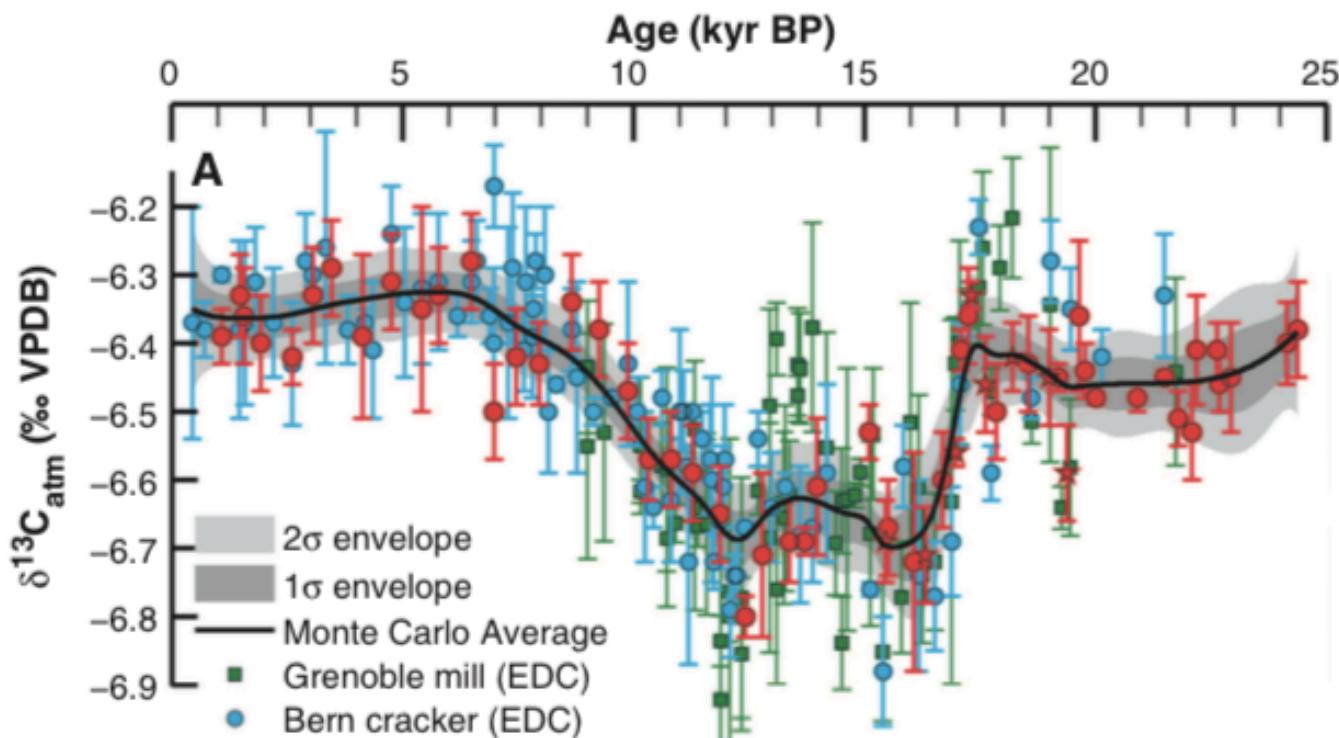


$$\begin{aligned} O(t) + S(t) - R_P(t) &= R_A(t) \\ \Rightarrow O(t) + S(t) &= R_P(t) + R_A(t) \end{aligned}$$

Assume that the amount coming from the Deep Ocean and Biosphere is a convex combination:

$$\begin{aligned} O(t) &= \alpha(t)(R_P(t) + R_A(t)) \\ S(t) &= (1 - \alpha(t))(R_P(t) + R_A(t)) \end{aligned}$$

But we really need to know the ratio of ^{13}C to ^{12}C in the atmosphere.



Schmitt, J. et al. *Science*: 336 pg. 711-713.

Some Notation

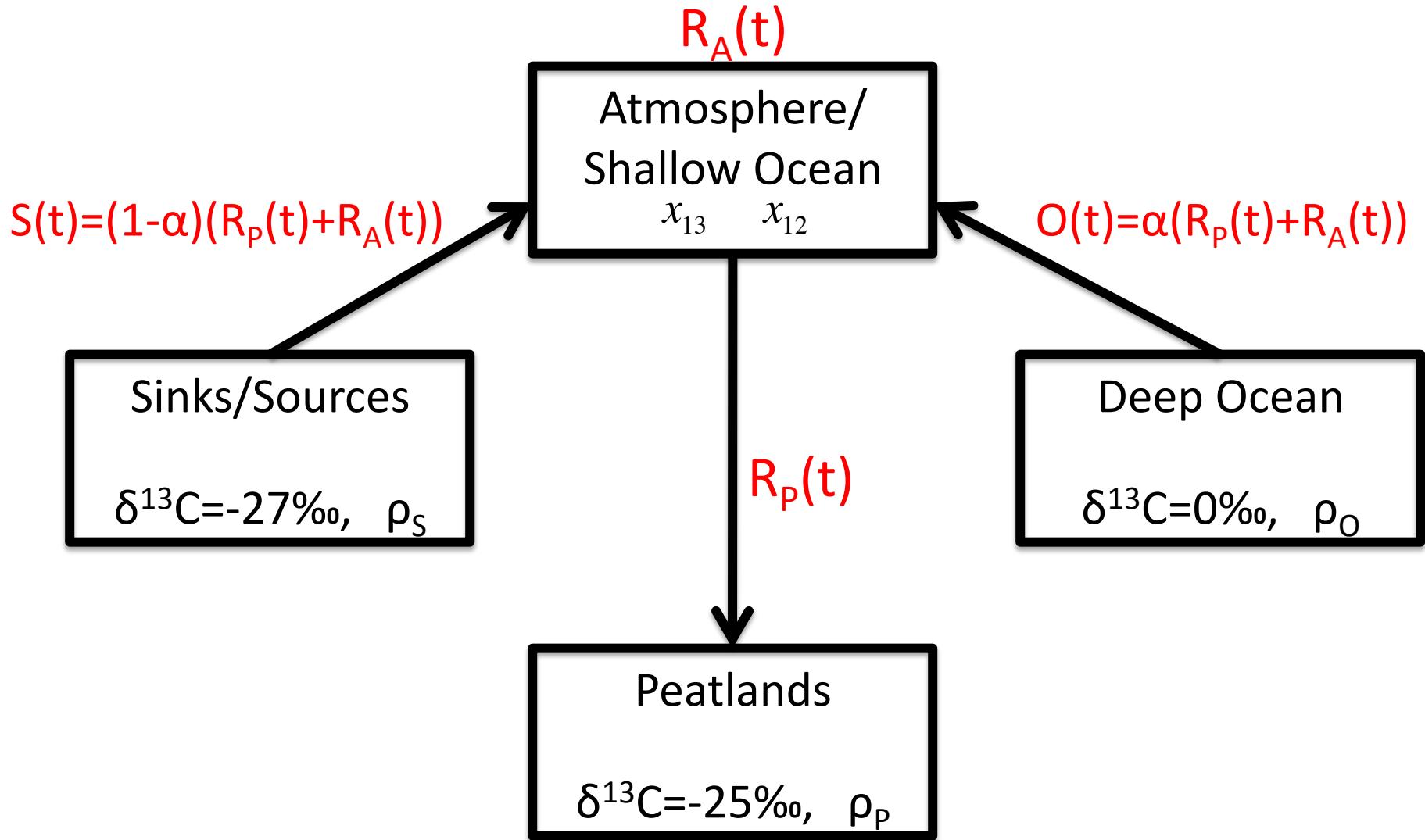
x_{13} := amount of ^{13}C in atmosphere

x_{12} := amount of ^{12}C in atmosphere

ρ_P := ratio of ^{13}C to ^{12}C in peat

ρ_O := ratio of ^{13}C to ^{12}C in the deep ocean

ρ_S := ratio of ^{13}C to ^{12}C in sinks/sources



“Out”

$$\omega'_{13}(t) = \frac{\rho_P}{1 + \rho_P} R_P(t)$$

$$\omega'_{12}(t) = \frac{1}{1 + \rho_P} R_P(t)$$

Notice that

$$\omega'_{13}(t) + \omega'_{12}(t) = R_P(t)$$

and at each $t=t_*$ we have

$$\frac{\omega'_{13}(t_*)}{\omega'_{12}(t_*)} = \rho_P$$

“In”

$$\eta'_{13}(\alpha, t) = \frac{\rho_s + \alpha(t)(\rho_o - \rho_s)}{1 + \rho_s + \alpha(t)(\rho_o - \rho_s)} (R_P(t) + R_A(t))$$

$$\eta'_{12}(\alpha, t) = \frac{1}{1 + \rho_s + \alpha(t)(\rho_o - \rho_s)} (R_P(t) + R_A(t))$$

Again

$$\eta'_{13}(\alpha, t) + \eta'_{12}(\alpha, t) = R_P(t) + R_A(t)$$

and at each $t=t_*$ we have

$$\frac{\eta'_{13}(\alpha, t_*)}{\eta'_{12}(\alpha, t_*)} = (1 - \alpha(t_*))\rho_s + \alpha(t_*)\rho_o$$

So that

$$x'_{13}(\alpha, t) = \eta'_{13}(\alpha, t) - \omega'_{13}(t)$$

$$x'_{12}(\alpha, t) = \eta'_{12}(\alpha, t) - \omega'_{12}(t)$$

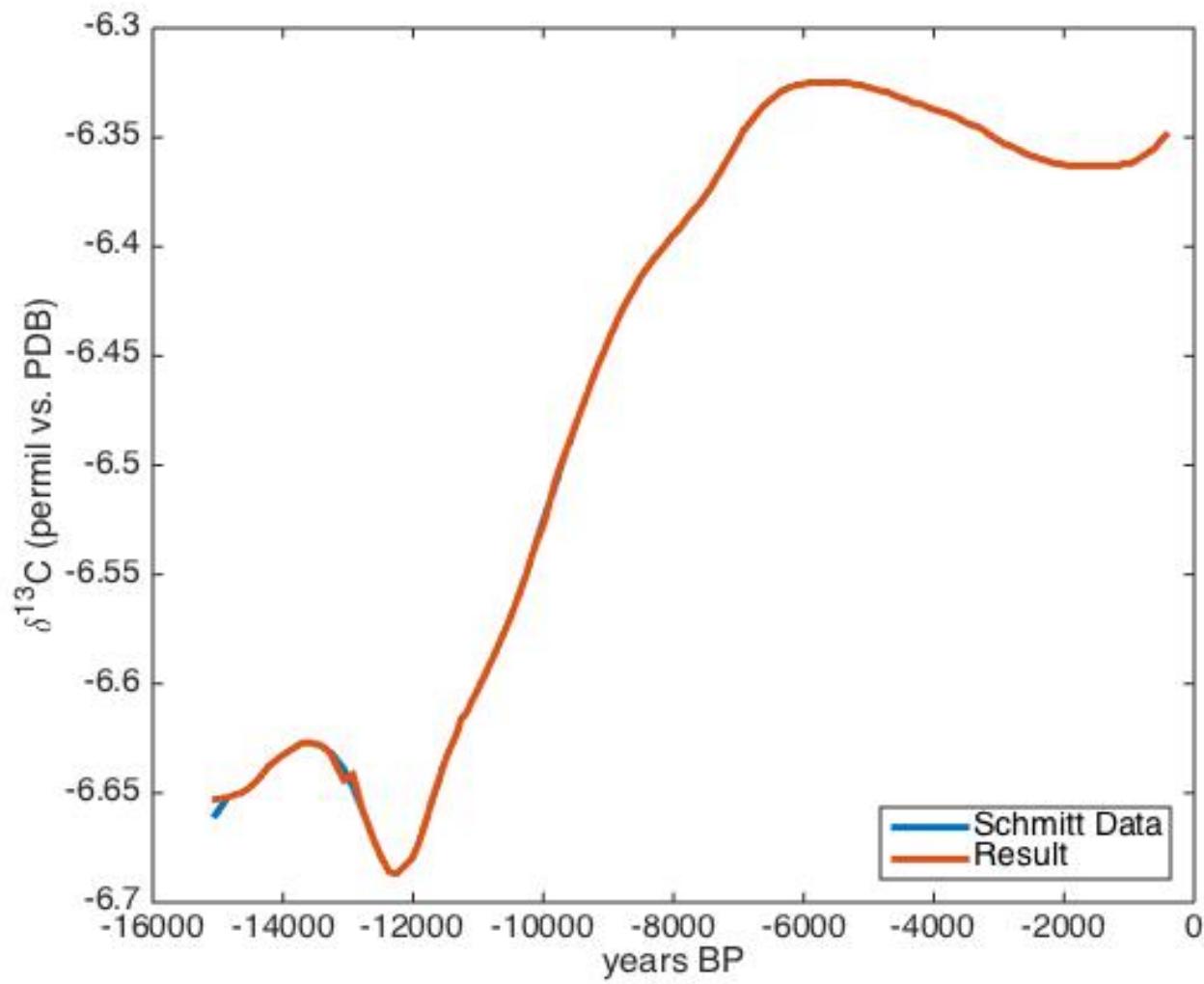
and

$$x_{13}(\alpha, t) = x_{13}(\alpha, t_0) + \int_{t_0}^t x'_{13}(\alpha, s) ds$$

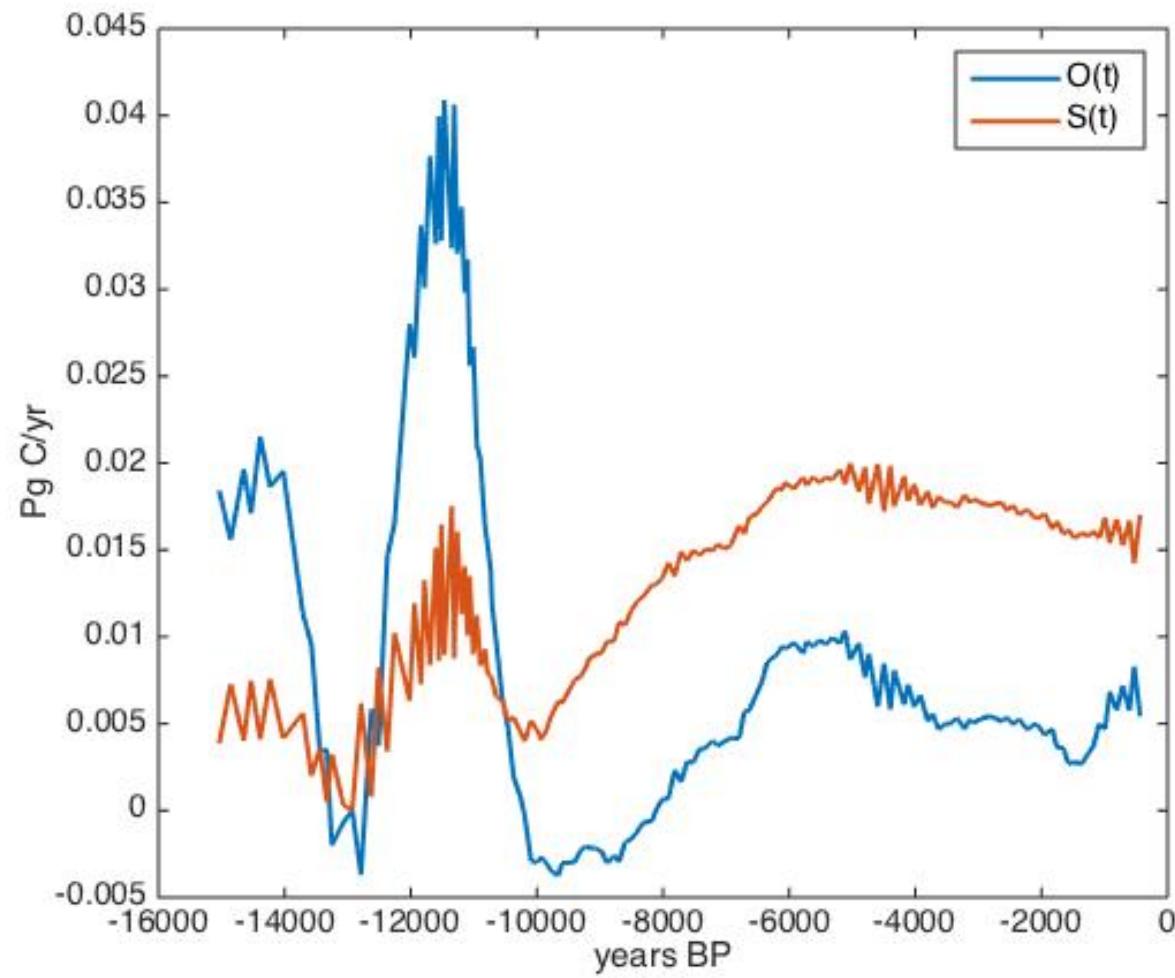
$$x_{12}(\alpha, t) = x_{12}(\alpha, t_0) + \int_{t_0}^t x'_{12}(\alpha, s) ds$$

We need to find the $\alpha(t)$ which reproduces Schmitt's data.

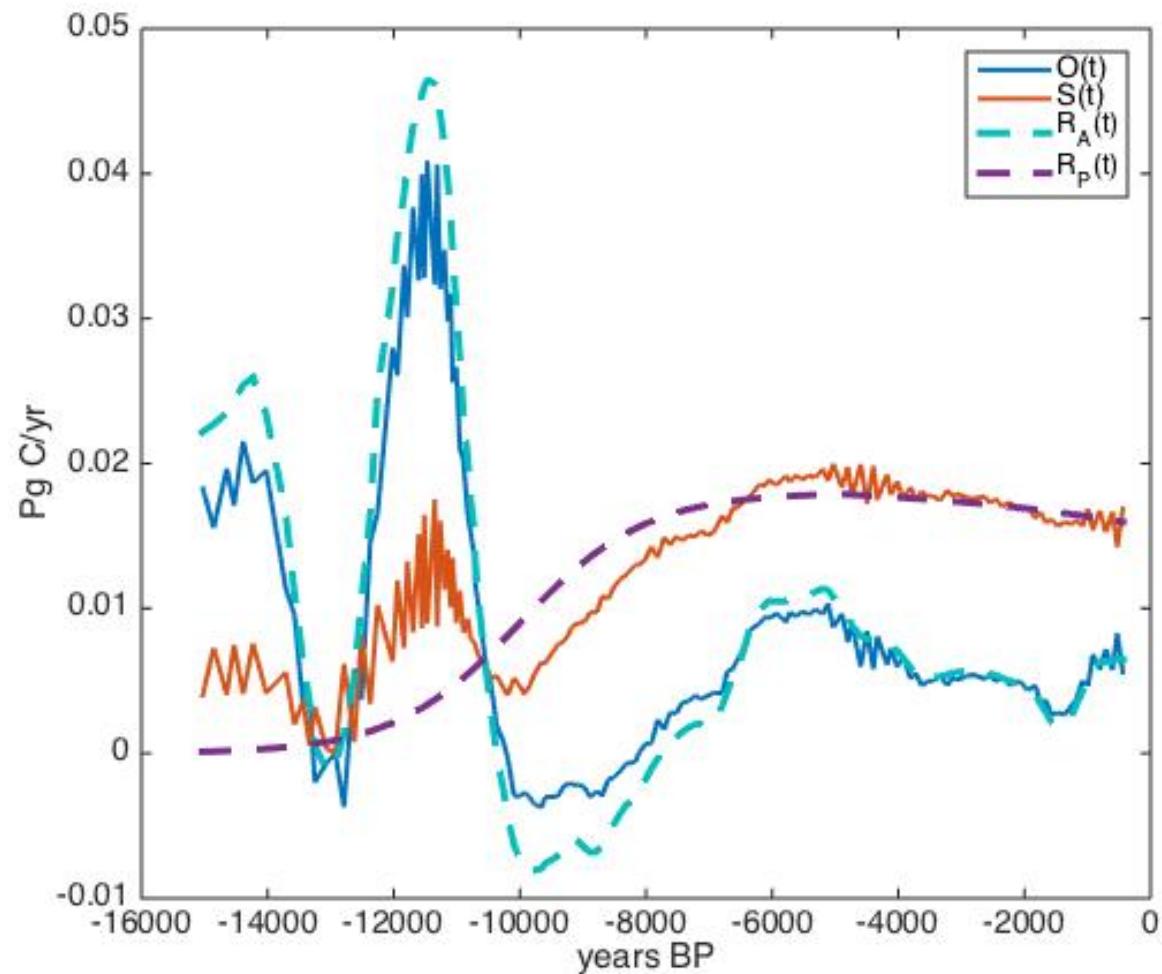
Results



Results



Results



References

- Brook, E. “The Ice Age Carbon Puzzle.”
Science: **336** pg. 682-683.
- Gorham, E. et al. “Long-term carbon sequestration in North American peatlands.”
Qua. Sci. Rev.: **58** pg.77-82.
- Schmitt, J. et al. “Carbon Isotope Constraints on the Deglacial CO₂ Rise from Ice Cores.”
Science: **336** pg. 711-713.