

**Due date:**

Friday, 3/12, **due 6pm, submit through Canvas.**

**Instructions:**

Students are encouraged to work together and discuss the homework problems, however each student must write up the solutions in their own words. Homework solutions should be well-explained, except True/False questions unless requested otherwise.

The format of HW is not restricted, but the PDF file is the preferred one.

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**Problem 1:** Suppose  $A$  is a  $n$ -by- $n$  matrix. Suppose that  $\mathbf{x}$  is a vector in  $\mathbb{R}^n$ . We define  $\|\mathbf{x}\|_2 = \sqrt{x_1^2 + \cdots + x_n^2}$ , where  $\mathbf{x} = (x_1, \cdots, x_n)$ . Find the operator norm of  $A = \begin{pmatrix} 1 & 0 \\ 0 & -5 \end{pmatrix}$ . That is, find  $\|A\|_2 = \max\{\|A\mathbf{u}\|_2 : \|\mathbf{u}\|_2 = 1\}$ .

**Problems in [1]:**

Pages 141–142, problems 3.2.16, 3.2.17 (only do 3.2.16 for this weighted inner product), 3.2.27

Pages 147–148, problems 3.3.4

Pages 149–150, problems 3.3.20(a-d), 3.3.28(a-b)

Pages 155–155, problems 3.3.45(d)

Pages 159–161, problems 3.4.1(c,e), 3.4.6, 3.4.7(a)

Pages 165–166, problems 3.4.22(a,b) for (iv), 3.4.27

**References**

- [1] Peter Olver and Chehrzad Shakiban, Applied Linear Algebra, 2<sup>nd</sup> Edition